

MCA DEGREE I SEMESTER EXAMINATION DECEMBER 2013

CAS 2105 COMPUTER BASED OPTIMIZATION

(Regular and Supplementary – 2011 Revision)

Time: 3 Hours

Maximum Marks: 50

PART A

(Answer ALL questions)

(15 × 2 = 30)

- I. (a) Define basic solution and optimum basic feasible solution.
 (b) Briefly explain big-M method for solving LPP.
 (c) Solve graphically.
 Maximize $Z=5X_1+4X_2$
 Subject to $6X_1+4X_2 \leq 24$
 $X_1+2X_2 \leq 6$
 $X_2 \leq 2$
 $X_2-X_1 \leq 1$
 and $X_1, X_2 \geq 0$
- II. (a) Explain MODI method for testing the optimality of transportation problem.
 (b) Formulate the mathematical model of assignment problem.
 (c) What is degeneracy in transportation problem?
- III. (a) Give branch and bound algorithm to solve integer programming problem.
 (b) Explain the characteristics of 0-1 integer programming problem.
 (c) Differentiate pure integer programming and mixed integer programming.
- IV. (a) State Bellman's principle of optimality.
 (b) With suitable example explain probabilistic dynamic programming.
 (c) What is Markovian property?
- V. (a) List and explain the components of a Queuing system.
 (b) Define stochastic process and list its classification.
 (c) Write notes on pure birth process and pure death process, give examples for each.

PART B

(5 × 4 = 20)

- VI. Use simplex method to solve
 Maximize $Z=4X_1+10X_2$
 Subject to $2X_1+X_2 \leq 50$
 $2X_1+5X_2 \leq 100$
 $2X_1+3X_2 \leq 90$
 and $X_1, X_2 \geq 0$

OR

- VII. Apply dual simplex method to solve
 Minimize $Z=3X_1+X_2$
 Subject to $X_1+X_2 \geq 1$
 $2X_1+3X_2 \geq 2$
 and $X_1, X_2 \geq 0$

(P.T.O.)

VIII. Solve the transportation problem by Vogel's approximation method.

	D1	D2	D3	D4	Supply
S1	3	7	6	4	5
S2	2	4	3	2	2
S3	4	3	8	5	3
Demand	3	3	2	2	

OR

IX. Solve the assignment problem by Hungarian algorithm.

	A	B	C	D	E
1	30	37	40	28	40
2	40	24	27	21	36
3	40	32	33	30	35
4	25	38	40	36	36
5	29	62	41	34	39

X. Solve the integer programming problem by Gomory's fractional cut method.

$$\begin{aligned} &\text{Maximize } Z = X_1 + 4X_2 \\ &\text{Subject to } 2X_1 + 4X_2 \leq 7 \\ &\quad \quad \quad 5X_1 + 3X_2 \leq 15 \\ &\quad \quad \quad \text{and } X_1, X_2 \geq 0 \end{aligned}$$

OR

XI. Solve the Traveling Salesman's problem by branch and bound method.

	A	B	C	D	E
A	-	4	7	3	4
B	4	-	6	3	4
C	7	6	-	7	5
D	3	3	7	-	7
E	4	4	5	7	-

XII. Divide a positive quantity C into n equal parts so as to maximize their product.

OR

XIII. Use dynamic programming problem to solve.

$$\begin{aligned} &\text{Maximize } Z = 3X_1 + 5X_2 \\ &\text{Subject to } X_1 \leq 4 \\ &\quad \quad \quad X_2 \leq 6 \\ &\quad \quad \quad 3X_1 + 2X_2 \leq 18 \\ &\quad \quad \quad \text{and } X_1, X_2 \geq 0 \end{aligned}$$

XIV. Write short notes on:

- (i) jokeying
- (ii) service utilization factor
- (iii) reneging
- (iv) balking

OR

XV. A television repairman finds that the time spend on his jobs has an exponential distribution with mean 30 minutes. If he repairs the sets in the order they came in and if the arrival follows poisson distribution with an average rate of 10 per 8 hours day. Calculate the repairman's idle waiting time and expected number of TV sets in the system.
