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MCA DEGREE I SEMESTER EXAMINATION NOVEMBER 2014

CAS 2101 COMBINATORICS AND GRAPH THEORY
(Supplementary)

Time: 3 Hours

Maximum Marks: 50

PART A
(Answer ALL questions)

(15 × 2 = 30)

- I. (a) State the principle of inclusion and exclusion.
(b) Define Rook polynomial.
(c) Find the coefficient of x^2y^4 in the expansion of $(x+y)^6$.
- II. (a) Define Steiner system.
(b) Prove that if V is even then λ is even, for a design with $b = v$.
(c) What do you mean by Hadamard matrix.
- III. (a) Define isomorphism in graph theory.
(b) What do you mean by traveling salesman problem.
(c) Prove that the number of vertices of odd degree in a graph is always even.
- IV. (a) Distinguish between incidence matrix and adjacency matrix in graphs.
(b) Define Planar graph.
(c) State the five color theorem.
- V. (a) Define Arborescence.
(b) State Cayley's theorem.
(c) What do you mean by 'connectedness' in graph theory?

PART B

(5 × 4 = 20)

- VI. Solve the recurrence relation $a_n - 5a_{n-1} + 6a_{n-2} = 2$, by method of generating function with the boundary condition $a_0 = 1, a_1 = 1$.
OR
- VII. Prove that

$$\binom{n+1}{r+1} = \binom{n}{r+1} + \binom{n-1}{r} + \binom{n-1}{r-1}$$
- VIII. Show that in a block design,
 $r(k-1) = \lambda(v-1)$ and $bk = vr$.
OR
- IX. Briefly explain the error correcting code with an example.
- X. Prove that a connected graph is an Euler graph iff all vertices are of even degree.
OR
- XI. State and prove Max-flow. Min-cut theorem
- XII. Prove that a graph with n vertices is a complete graph iff its chromatic polynomial is
 $P_n(\lambda) = \lambda(\lambda-1)(\lambda-2)\dots(\lambda-n+1)$
OR
- XIII. Prove that a connected planar graph with n vertices and e edges has $e-n+2$ regions.
- XIV. Prove that the number of simple, labelled graph with n vertices is $2^{\frac{n(n-1)}{2}}$.
OR
- XV. Prove that there are n^{n-2} labelled trees having n vertices ($n \geq 2$).